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TO BRA Subset Sum is NP-Hard. Reduction: Vertex Cover Input: Graph G & size k Goal: find k vertices, such that even edge in G is incident to at least one vertex in set Challenge: Construct a set of numbers, s.t. we can hit a target value G) G has that of size k vertex over

Recall: base 4 $(32012)_{4} = 34+2.4+0.4+1.4+2.40$ 1032+2312 >10010 TTT IS Idea: Use base 4: force a target T that requires you to use only vertices, but to "cover" edges Number edges O. E-1 a create a number for subset sum WE digits Co: 20 -00. -010C, : b1700 QE-1: PE-1=010-0, E Spots 55)

For each vertex, make another # Q_{1} , \tilde{c} = 1 els Think of base 4 representation \widehat{V} $a_u := 11000_4 = 1344$ $b_{\mu\nu} := 010000_4 \ge 256$ $a_{v} := 110110_{4} = 1300$ $b_{uw} := 001000_4 = 64$ $a_w := 101101_4 = 1105$ $b_{vw} := 000100_4 =$ 16 $a_x := 100011_4 = 1029$ $b_{vx} := 000010_4 =$ $b_{wx} := 000001_4 =$

Now, set T= k.4^E+ 204ⁱ inpat L=0 2 each Ares Kvortees Proof: Size & VCZ=> Sum to T DVC: JE vertices V1, V2, -, VK s.t. teeE, e is incident to some $V_{\tilde{c}} \in \{ \langle V_{1}, \dots, V_{k} \}$

 \Longrightarrow (cont) Pick a subset:

E: Suppose some subset of Sums to T. options? Reall: T= k.4 = 5-1 0 204 Flus: Each digit position has only 3 1's across all #5;

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farthoo: Given $X = \{X_{1}, \dots, X_{n}\}, Can$ we pertition X into A+B $(SO A UB = X, A \cap B = \Phi, + A, B \neq \Phi)$ Z-Xi Z Xj X, EB XiEA Reduction

Proof;	· · · ·
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examples

arXiv.org > cs > arXiv:1203.1895 Search or Article ID inside arXiv All papers Computer Science > Computational Complexity Computer Science > Computational Complexity Dow Classic Nintendo Games are (Computationally) Hard - PD Greg Aloupis, Erik D. Demaine, Alan Guo, Giovanni Viglietta Ucree (Submitted on 8 Mar 2012 (v1), last revised 8 Feb 2015 (this version, v3)) Curre We prove NP-hardness results for five of Nintendo's largest video game franchises: Mario, Donkey Kong, Legend of Zelda, Metroid, and Pokemon. Our results apply to generalized versions of Super Mario Bros. 1- - Oth 3, The Lost Levels, and Super Mario World; Donkey Kong Country 1-3; all Legend of Zelda games; all Chan Metroid games; and all Pokemon role-playing games. In addition, we prove PSPACE-completeness of the Donkey Kong Country games and several Legend of Zelda games. Refer Subjects: Computational Complexity (cs.CC); Computer Science and Game Theory (cs.GT) NA Cite as: arXiv:1203.1895 [cs.CC] For this version) Bublicsion history Bisli From: Alan Guo (view email) Gre [v1] Thu, 8 Haz 2012 19:37:20 GMT (627kb,D) Ja [v2] Thu, 6 Feb 2014 18:24:15 GMT (3330kb,D) Ala Booki Ala Booki Ima Wh											
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shes until it is collected by Mario.

11 of 36



Figure 11: Clause gadget for Super Mario Bros.

Link back to: arXiv, form interface, contact.





Left: Start gadget for Super Mario Bros. Right: The item block contains a



Figure 9: Finish gadget for Super Mario Bros.



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Help | Adv

Computer Science > Computational Geometry

On the complexity of optimal homotopies

Erin Wolf Chambers, Arnaud de Mesmay, Tim Ophelders

(Submitted on 2 Nov 2017)

In this article, we provide new structural results and algorithms for the Homotopy Height problem. In broad terms, this problem quantifies how much a curve on a surface needs to be stretched to sweep continuously between two positions. More precisely, given two homotopic curves γ_1 and γ_2 on a combinatorial (say, triangulated) surface, we investigate the problem of computing a homotopy between γ_1 and γ_2 where the length of the longest intermediate curve is minimized. Such optimal homotopies are relevant for a wide range of purposes, from very theoretical questions in quantitative homotopy theory to more practical applications such as similarity measures on meshes and graph searching problems.

9

We prove that Homotopy Height is in the complexity class NP, and the corresponding exponential algorithm is the best one known for this problem. This result builds on a structural theorem on monotonicity of optimal homotopies, which is proved in a companion paper. Then we show that this problem encompasses the Homotopic Fréchet distance problem which we therefore also establish to be in NP, answering a question which has previously been considered in several different settings. We also provide an O(log n)-approximation algorithm for Homotopy Height on surfaces by adapting an earlier algorithm of Har-Peled, Nayyeri, Salvatipour and Sidiropoulos in the planar setting.

S Droble any prento) runing

Liveer program In a linear program, we are given a Set of variables The goal is to give these real values So that: Due satisfy some set of linear equations or inequalities 2 We maximize or minimize some linear objective function

Example LP: Cargo plane: - can carry 100 tons, + volume of 60 cubic meters - 3 metericls: · 1st: 2 tons/cubic neter, 40 cubic meters available, worth \$ 1000 per com ozna: 1 ton/c.m, 30 cm total available, and worth \$1200 per 3rd. 3 tons/cm, 20 cms total, d \$12,000 per C.M

Profit.maximize Such that! $X_1 \leftarrow$ XZ X35

etry: Each equation makes a plane (since linear! Georetr 121 -) ·~

Each vorable adds a dinension: Maximize X,+6x2+BX3 $X_{1} \leq 200$ $X_{2} \leq 300$ $X_{1} + X_{2} + X_{3} \leq 400$ $\chi_{2} + 3\chi_{3} \leq 600$ $\chi_1 \ge O \otimes$ $\chi_2 \ge 0$ X2 20 And each egn adds a face to poly hedron

Another (more general) n foods, m numents Let $a_i = amount of nutrient i in food j$ $<math>r_i = requirement of nutrient i$ $<math>\chi_i = amount of food j purchased$ C; = cost of food j Goal: Buy food so you satisfy nutrients while minimizing cost matrix Can view as

 $7 \quad \overline{r} = (r_1, r_2, - r_m)$**...** H = . . . $\overline{\chi} = (\chi_1, \ldots, \chi_n)$ $C = (C_1, \dots, C_N)$ So: MINIMIZE 2.1.

In general, get systems like this: maximize $\sum c_j x_j$ subject to $\sum a_{ij}x_j \le b_i$ for each $i = 1 \dots p$ $\sum a_{ij} x_j = b_i \quad \text{for each } i = p + 1 \dots p + q$ $\sum a_{ij} x_j \ge b_i \quad \text{for each } i = p + q + 1 \dots n$

Geometric picture:



A two-dimensional polyhedron (white) defined by 10 linear inequalities.

Canonical formi Avoid having both = and Why Soget something more like our first example: maximize $\sum_{i=1}^{a} c_j x_j$ subject to $\sum_{i=1}^{n} a_{ij} x_j \le b_i$ for each i = 1 ... n $x_j \ge 0$ for each $j = 1 \dots d$ Or, given a vertor è, matrix A + vector b:

Anything can be put into Canonical Forme The reduction: (DAvoid = -(2) Avoid \geq

How could these not have a solution? Maximize XI+X2 2 ways

Ichires ~ (* S~

maximize x - ysubject to $2x + y \le 1$ $x + y \ge 2$ $x, y \ge 0$





Note: O Multiplying by -1 turns any maximization problem into a minimization one: (1)2) Can turn inequalities into equalities via slack variables: $Saixi \leq b \Rightarrow$

3) Can change equalities into inequalities, also $Za_i X_i = b$ 1 = 1

Re algorithm: Simplex Assumes Canonical form maximize $\sum_{j=1}^{d} c_j x_j$ subject to $\sum_{i=1}^{u} a_{ij} x_j \le b_i$ for each i = 1..n $x_j \ge 0$ for each $j = 1 \dots d$ only for all variables

How to	implement, plus	runture;

Connections to other problems: It turns out that LPs are powerful chough to express many types of problems." In a sense, we solve many problems by reducing them to an LP:

Ex: Flows + Cuts Input: directed 6 w/edge capacities (le) $4S, t \in V$ Goal: Compute flow f:E=>IR S.t. 1) 04 fe) 4 de) $2 \forall \forall v \neq s, t,$ $\int f(h \rightarrow v) = \int f(v \rightarrow w)$ Make an LP: Maximize 5. t.

Related: Min cuts (S,T) Use indicator variables: $S_v = 0$ or 1 Xe=X(u=v)=1 if ues and veT 1

> want LP: The l Minimize Z. Cu-zu·Xu->v $X_{u \to v} + S_v - S_u \ge O$ $S_s = 1$ St 0 -

Note! For flow/cuts, a solution would yield optimal LP solution. The perese is not obvious! LP might have strange fractional answer which doesn't describe a cut. If can be shown that this won't happen (> but not obvious...