

# Hash Tables and Maps

## CSCI 2100 Data Structures

Spring 2018

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— EST. 1818 —

# STL Containers

- Sequence Containers – store sequences of values
  - vector, deque, list
- Associative Containers – use “keys” to access data rather than position (Account #, ID, SSN, ...)
  - set
  - multiset
  - map
  - multimap
- Container Adapters – specialized interfaces to general containers
  - stack, queue, priority\_queue

# Associative Containers

- Stores elements based on a key
- Key can consist of one or more attributes to uniquely identify each element (we will assume only one attribute).
- Example: Department of Motor Vehicles (DMV) uses license-plate # to identify a vehicle.
- Similar to vector & list – it is another storage structure with operations to access & modify elements.
- Main difference is that associative-container uses the key rather than an index (vector) or linear search (list) to retrieve an element.

# Associative-Container : set

- Stores a set of values (i.e., “keys”)
- Values are unique (stored only once)
- Implemented as a binary search tree
  - `#include <set>`
  - `set<string> s;`
- Fast insert and delete
  - `insert, erase`
- Fast search
  - `find`
- Other operations
  - `size, empty, clear, . .`

```
1 #include <iostream>
2 #include <set>
3 #include <string>
4
5 using namespace std;
6
7 int main() {
8     set<string> setOfNumbers;
9
10    // Lets insert four elements
11    setOfNumbers.insert("first");
12    setOfNumbers.insert("second");
13    setOfNumbers.insert("third");
14    setOfNumbers.insert("first");
15
16    // Only 3 elements will be inserted
17    cout<<"Set Size = "<<setOfNumbers.size()<<endl;
18
19    // Iterate through all the elements in a set and display the value.
20    for (set<string>::iterator it=setOfNumbers.begin(); it!=setOfNumbers.end(); ++it) {
21        cout << ' ' << *it;
22    }
23    cout<<"\n";
24
25    // Search for element in set using find member function
26    set<string>::iterator it = setOfNumbers.find("second");
27    if (it != setOfNumbers.end()) {cout<<"'first' found"<<endl;}
28    else {cout<<"'first' not found"<<endl;}
29
30    // Search for element in set using find member function
31    it = setOfNumbers.find("fourth");
32    if(it != setOfNumbers.end()) {cout<<"'fourth' found"<<endl;}
33    else {cout<<"'fourth' not found"<<endl;}
34
35    return 0;
36 }
```

# Associative Containers: multiset

- Stores a set of values (i.e., “keys”)
- Like set, but values need not be unique
- Implemented as a balanced binary search tree (red-black tree)
  - `#include <set>`
  - `multiset<string> ms;`
- Fast insert and delete
  - `insert, erase`
- Fast search
  - `find`
- Other operations
  - `size, empty, clear, . . .`

# Associative Containers: map

- Stores a set of (key, value) pairs
- Each key has one value
- Implemented as a binary search tree

```
#include <map>
//define a map with
//keys of type string
//and values of int
map<string, int> m;
```

- Fast insert and delete

```
m["Ted"] = 99;
insert, erase
```

"Ted" | 99

"Michael" | 105

"James" | 23

# Associative Containers: map

- Fast search

- `int x = m["Ted"];`
- `find`

- Other operations

- `size, empty, clear, . . .`



# STL Maps: Constructors

- Copy constructor:

```
map<char, int> m;
```

```
map<char, int> m2 (m) ;
```

# STL Maps: Data Storage

- An STL map is implemented as a tree-structure, where each node holds a “pair”
- Most important to know when retrieving data from the table
  - Some functions return the pair, not just the value
- A pair has two fields, *first* (holding the key) and *second* (holding the value)

# STL Map: Data Storage

- If you have a ***pair object***, you can use the following code to print the key and value:

```
cout << myPairObject.first << " " <<
    myPairObject.second;
```

- If you have a ***pointer to the pair object***, use the arrow operator instead

```
cout << myPairObject->first << " " <<
    myPairObject->second;
```

# STL Map: Data Storage

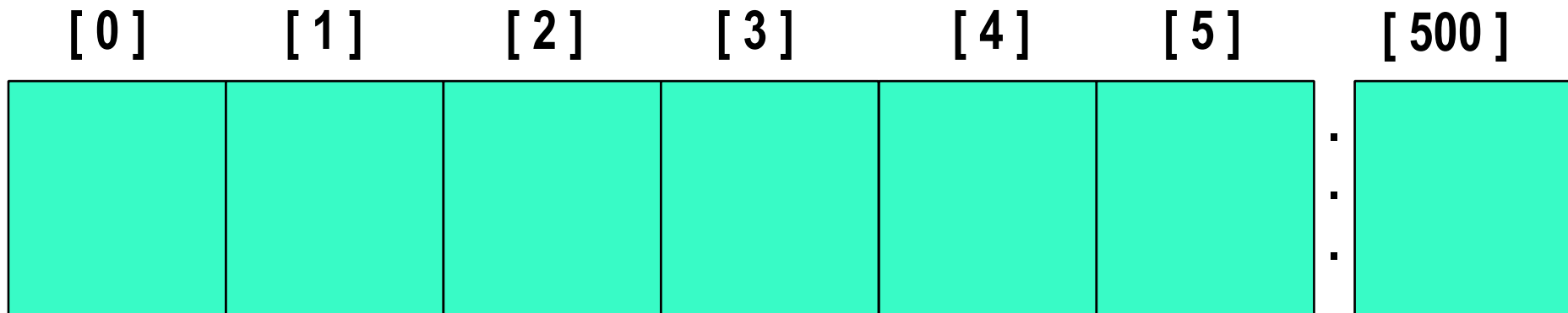
- Access element `at`
  - Returns a reference to the mapped value of the element identified with key `k`.
  - If `k` does not match the key of any element in the container, the function throws an `out_of_range` exception.
- Access element `[]`
  - If `k` matches the key of an element in the container, the function returns a reference to its mapped value.
  - If `k` does not match the key of any element in the container, the function inserts a new element with that key and returns a reference to its mapped value.

# StdMap.cpp

```
1 #include <iostream>
2 #include <string>
3 #include <map>
4
5 using namespace std;
6
7 int main () {
8     map<int,string> mymap;
9
10    mymap[1]="Banana";
11    mymap[2]="Peach";
12    mymap[3]=mymap[2];
13
14    cout << "mymap[1] is " << mymap[1] << '\n';
15    cout << "mymap[2] is " << mymap[2] << '\n';
16    cout << "mymap[3] is " << mymap[3] << '\n';
17
18    mymap.at(1) = "Melon";
19    mymap.at(2) = "Strawberry";
20    mymap.at(3) = "Kiwi";
21
22    map<int,string>::iterator it;
23    for (it=mymap.begin(); it!=mymap.end(); ++it)
24        cout << it->first << " => " << it->second << endl;
25
26    it = mymap.find(2);
27    if (it != mymap.end())
28        cout << "The value of the key [2] is " << it->second << endl;
29
30    return 0;
31 }
```

# What is a Hash Table?

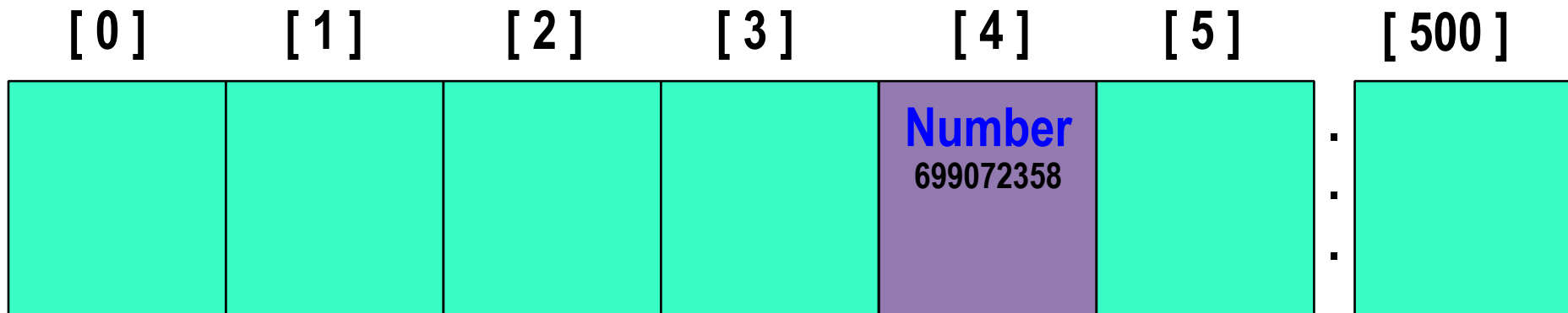
- The simplest kind of hash table is an array of records.
- This example has 501 records.



**An array of records**

# What is a Hash Table?

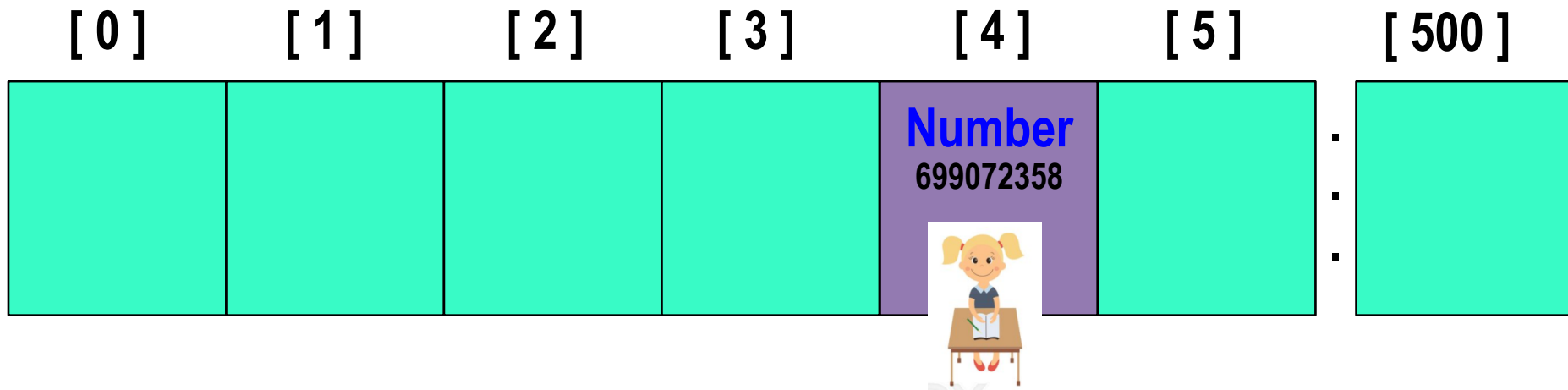
- Each record has a special field, called its **key**.
- In this example, the **key** is a long integer field called **Number**.



An array of records

# What is a Hash Table?

- The **Number** might be a person's identification number (e.g., student ID, SSN), and the rest of the record has information about the person.

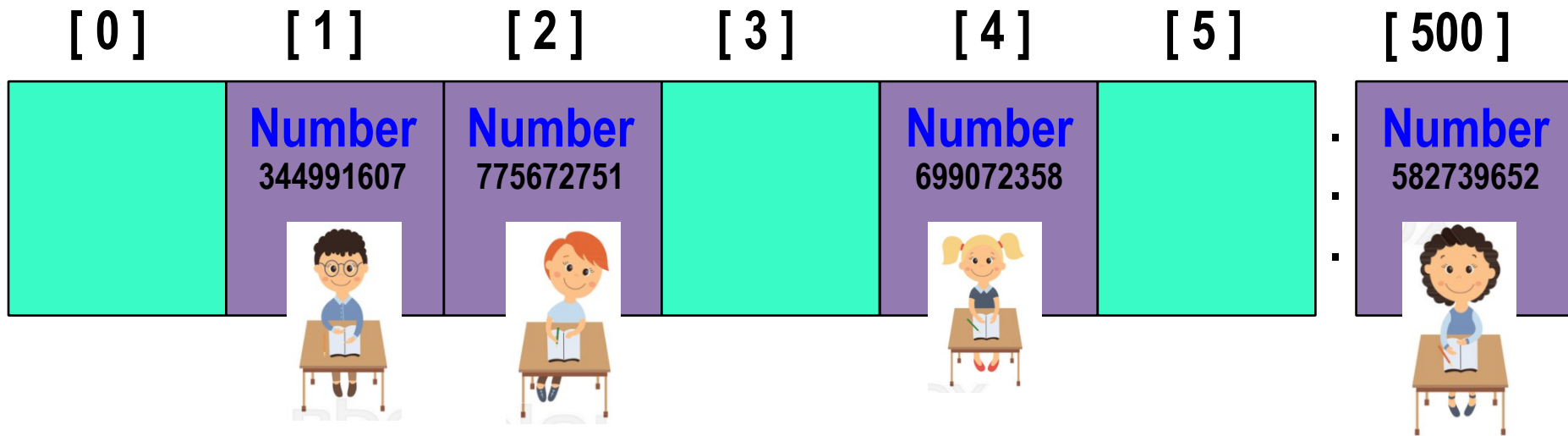


An array of records



# What is a Hash Table?

- When a hash table is in use, some spots contain valid records, and other spots are "empty".

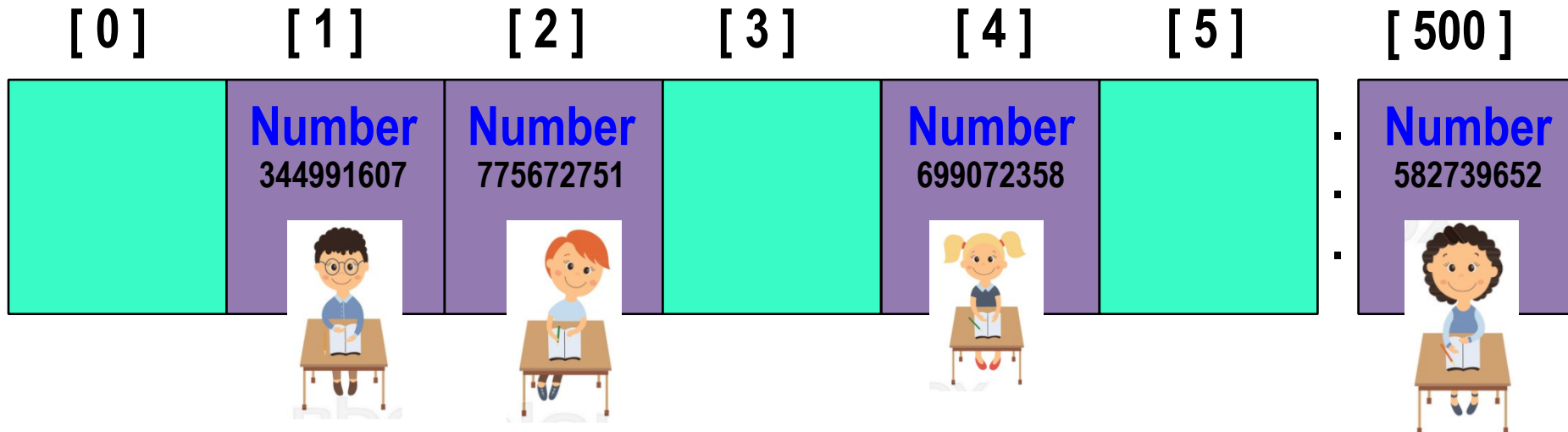


An array of records

# Inserting a New Record

- In order to insert a new record, the **key** must somehow be **converted to** an array **index**.
- The index is called the **hash value** of the **key**.

**Number**  
393802035

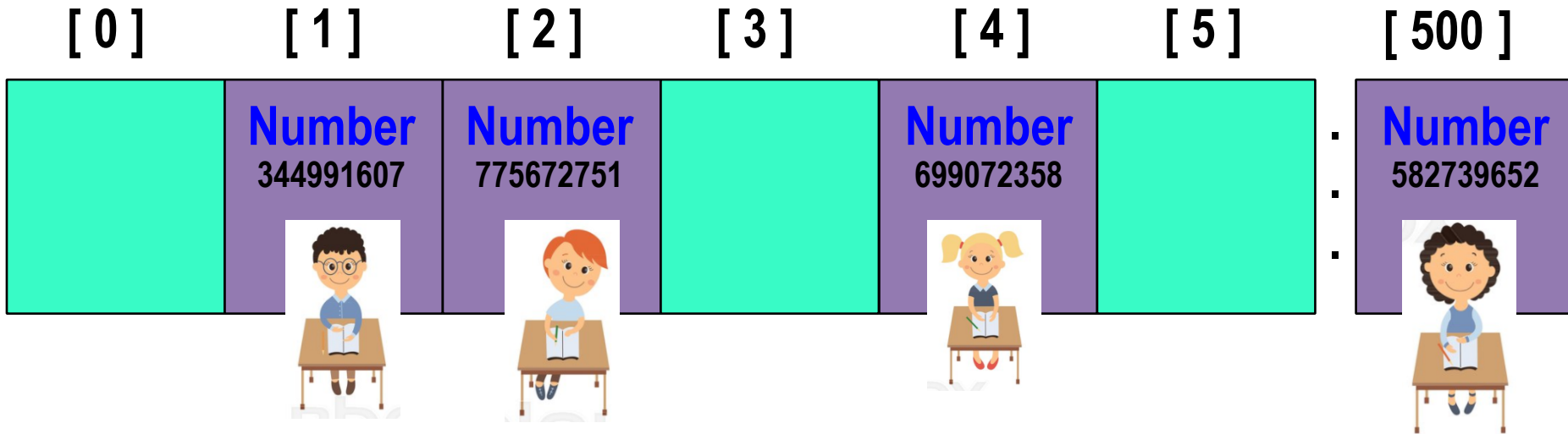


An array of records

# Inserting a New Record

- Typical way create a hash value:
  - Number mod ArraySize
  - $393802035 \text{ mod } 501 = 3$

Number  
393802035

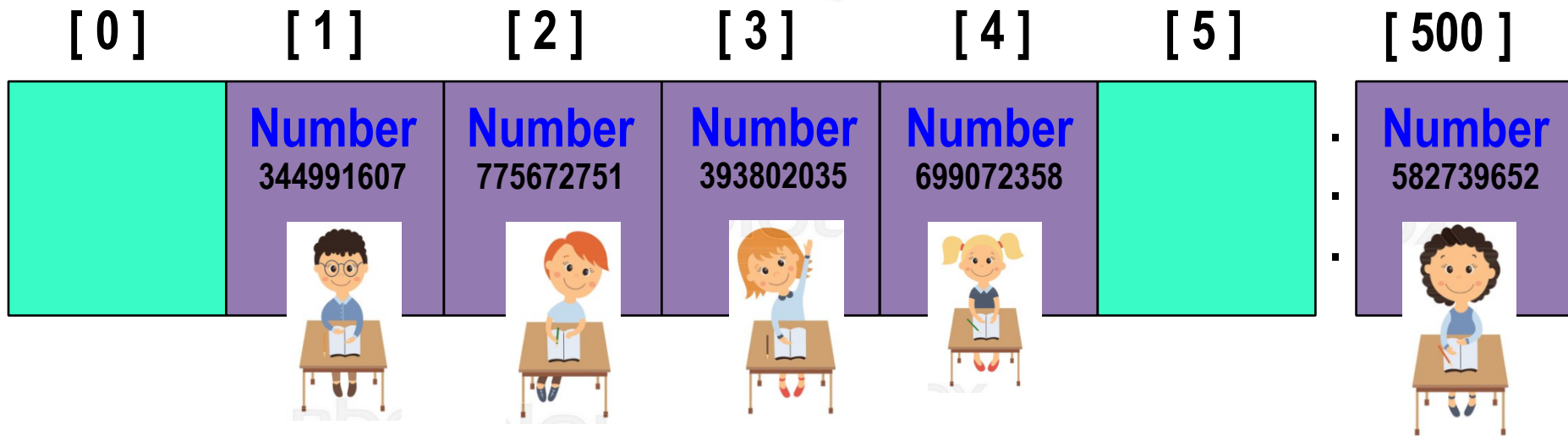
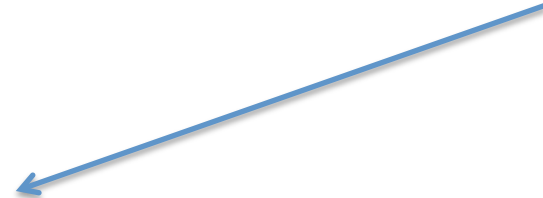


An array of records

# Inserting a New

- The **hash value** is used for the **location** of the new record.

**Number**  
393802035



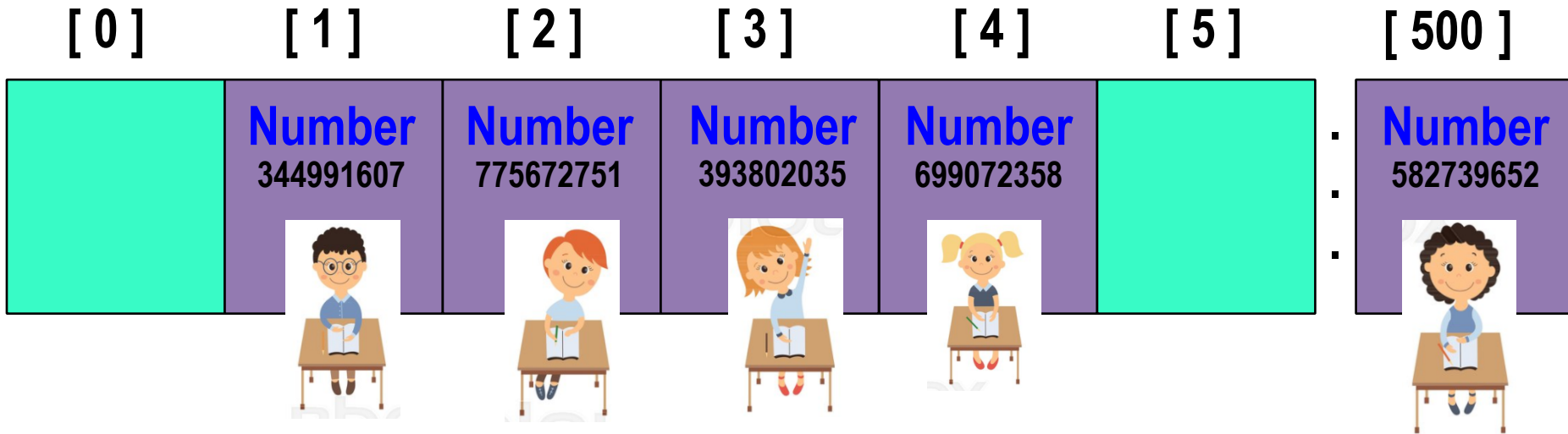
An array of records

# Hash Collisions

- Here is another new record to insert.

**Number**

493375785



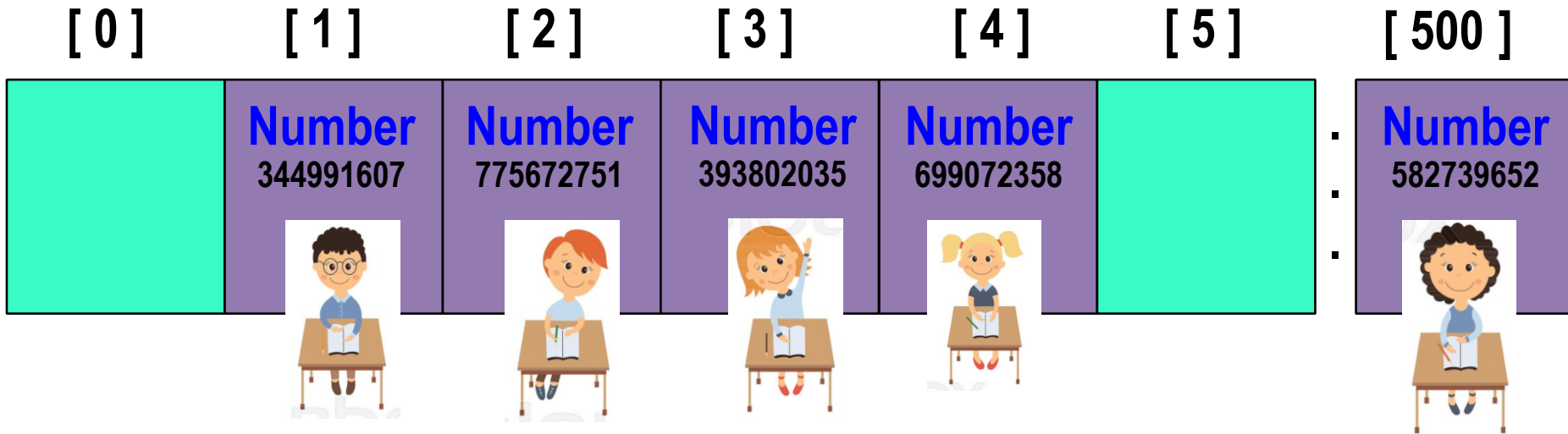
An array of records

# Hash Collisions

- Here is another new record to insert.
  - $493375785 \bmod 501 = 3$

**Number**

493375785

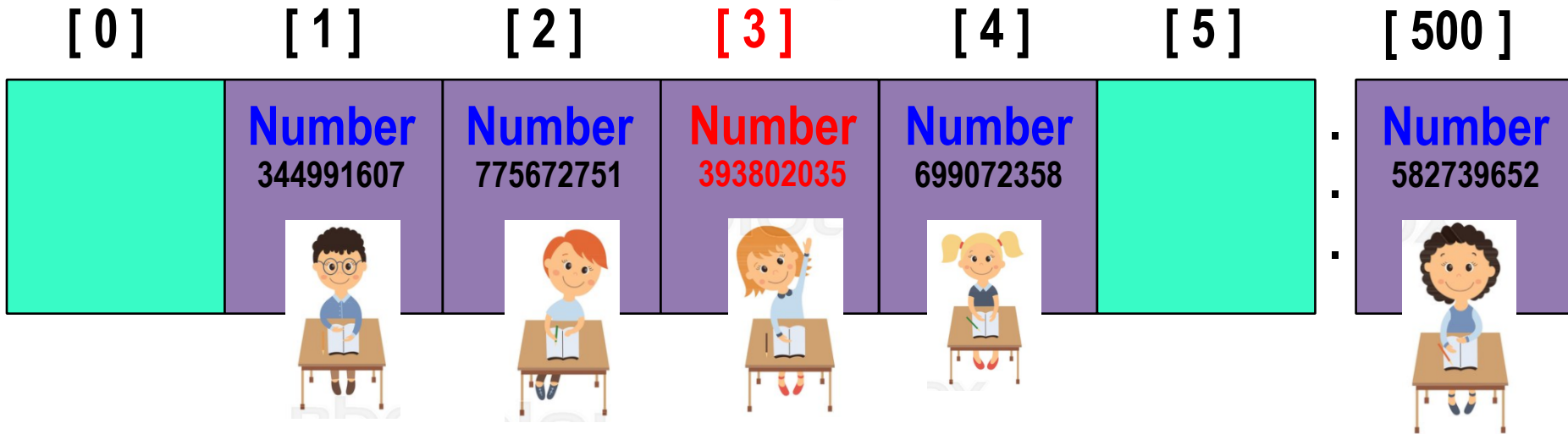
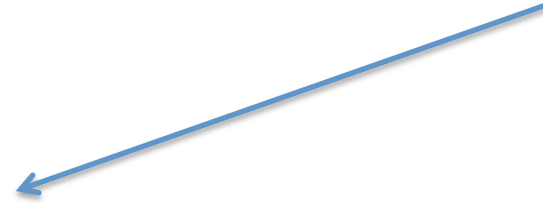


An array of records

# Hash Collisions

- Here is another new record to insert.
  - $493375785 \bmod 501 = 3$
  - Index **3** has already key and value.

**Number**  
493375785

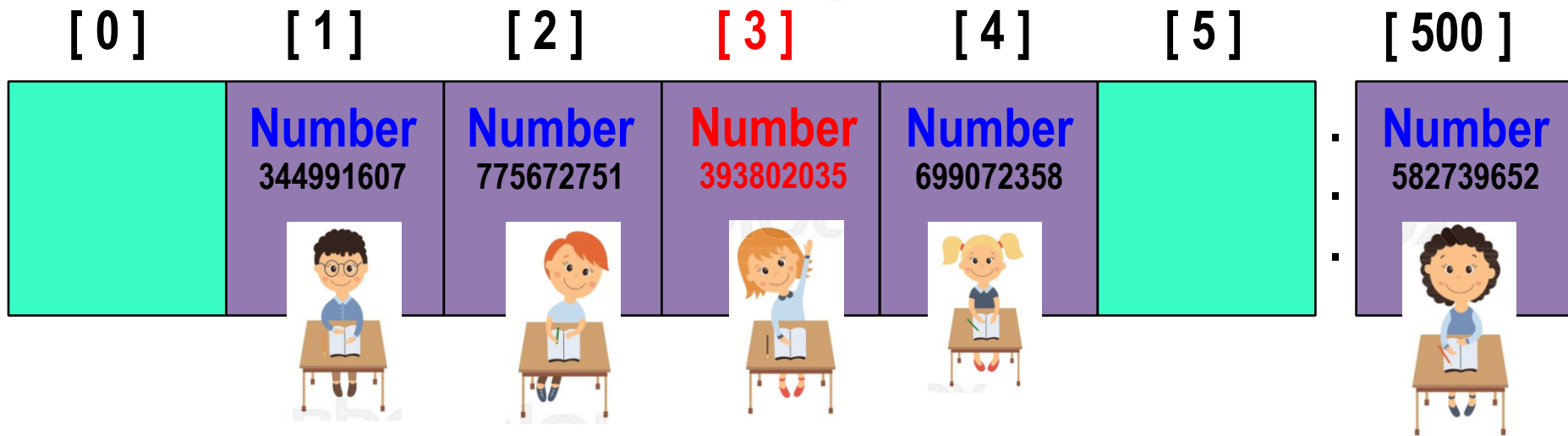


An array of records

# Hash Collisions

- This is called a **collision**, because there is already another valid record at [3].

Number  
493375785



An array of records

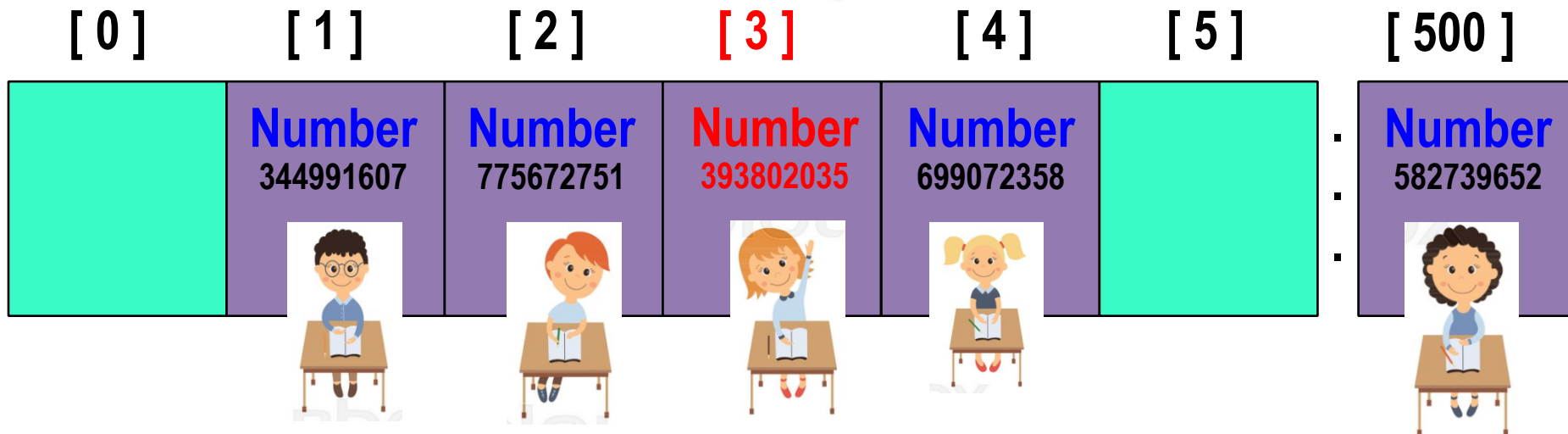


# Hash Collisions

- Let us make a collision rule:
  - When a collision occurs, move forward until you find an empty spot.

Number

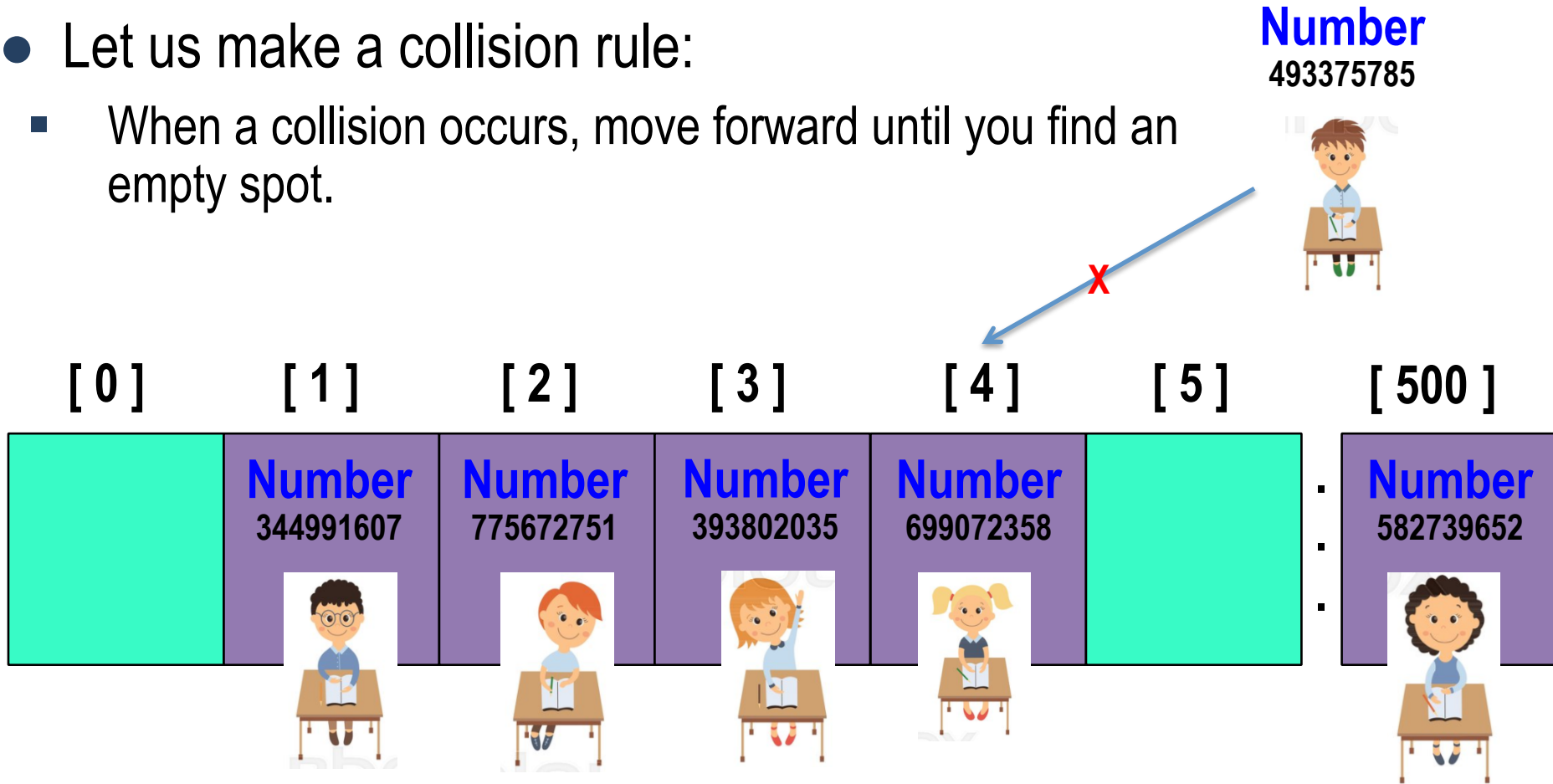
493375785



An array of records

# Hash Collisions

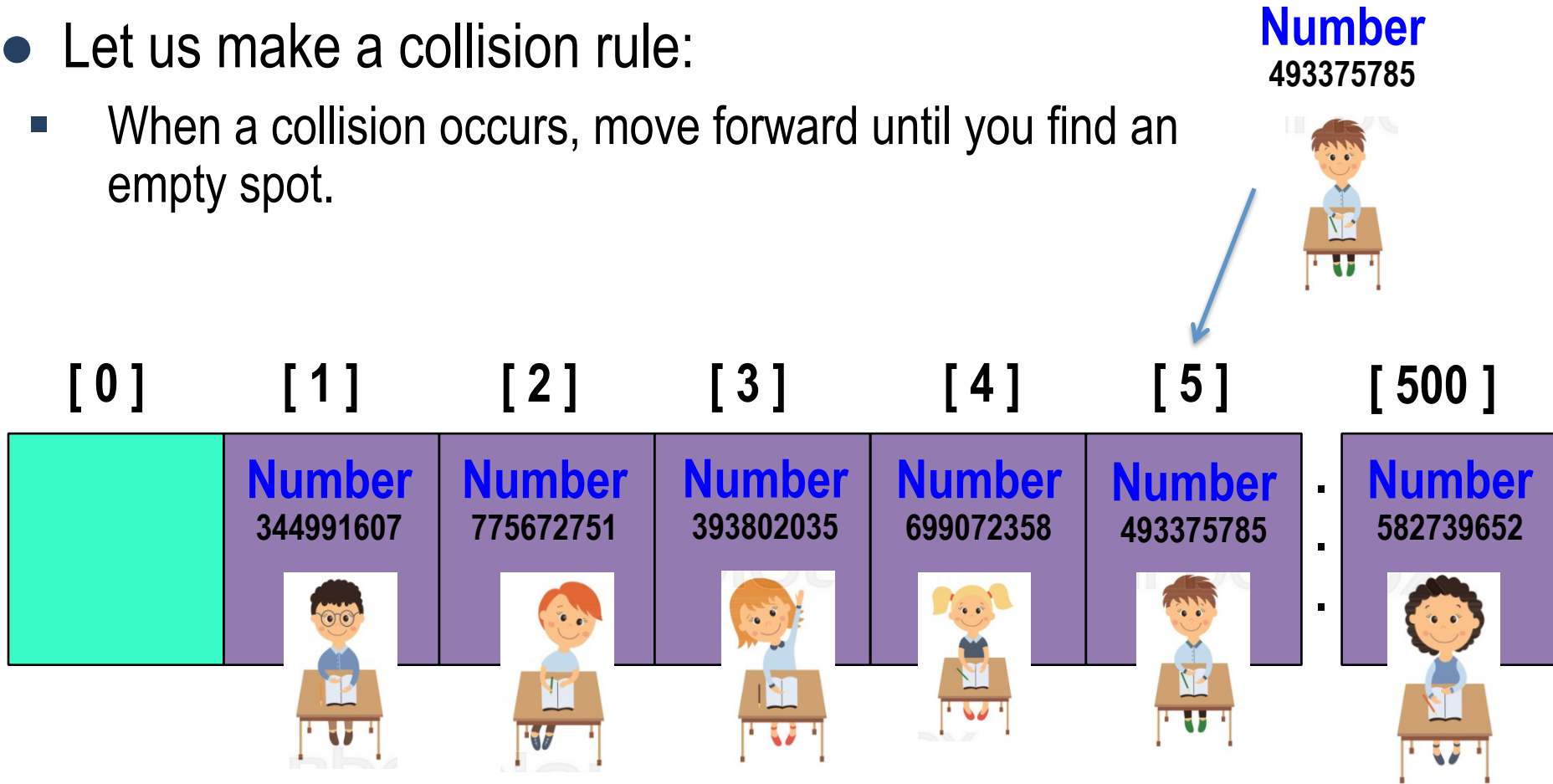
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An array of records

# Hash Collisions

- Let us make a collision rule:
  - When a collision occurs, move forward until you find an empty spot.

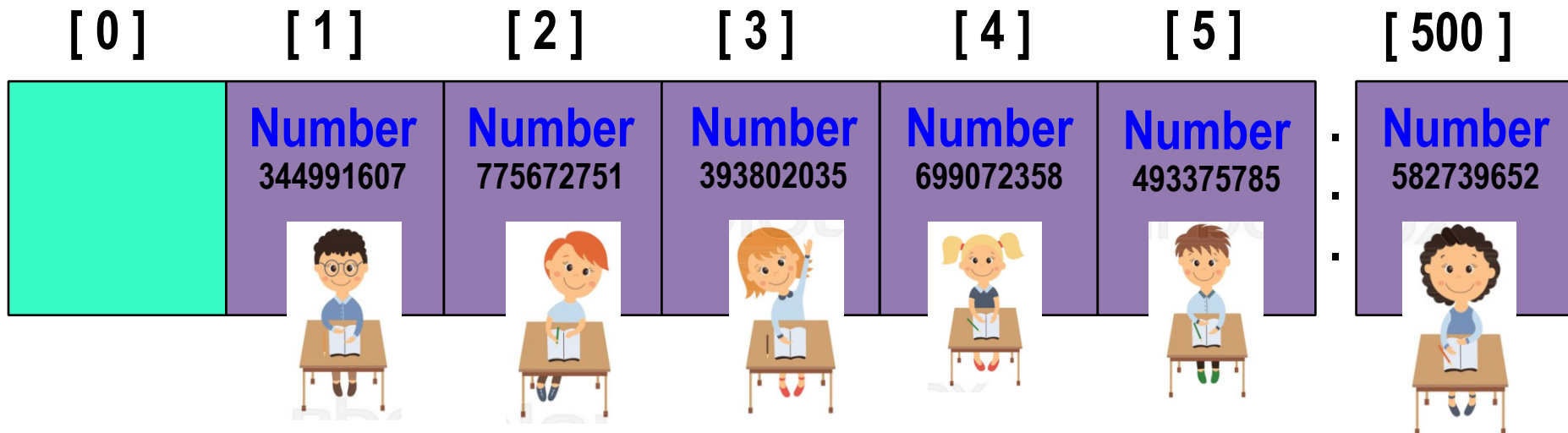


An array of records

# Searching for a Key

- The data (or value) that is attached to a key can be found fairly quickly.

**Number**  
493375785

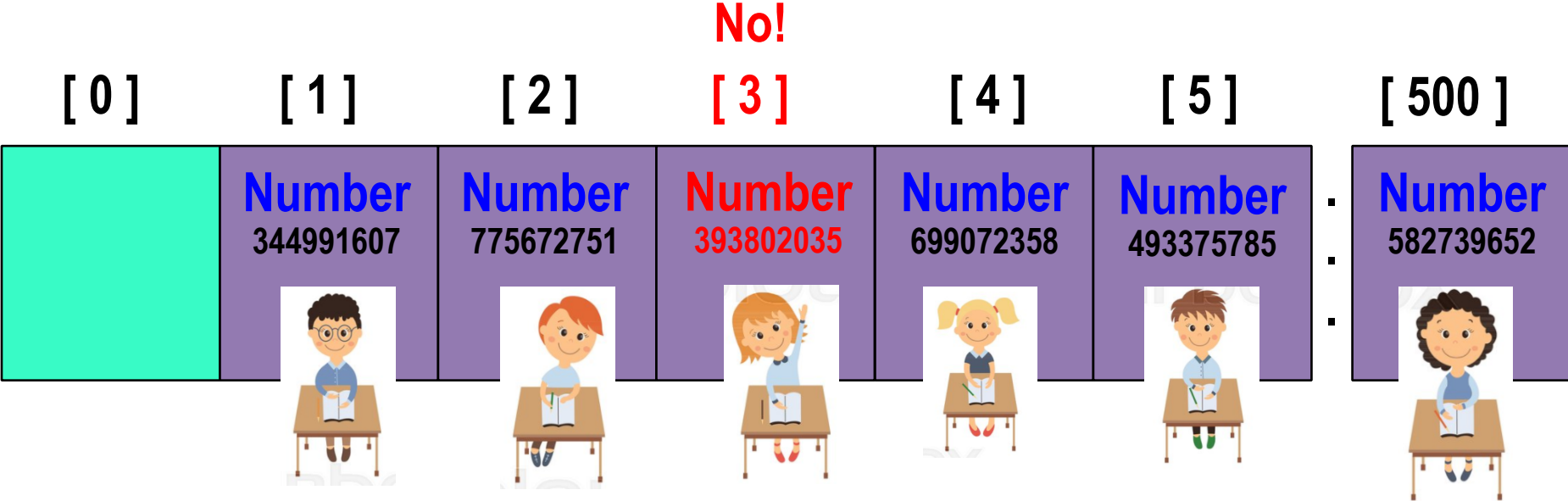


**An array of records**

# Searching for a Key

- The data (or value) that is attached to a key can be found fairly quickly.
  - $493375785 \text{ mod } 501 = 3$

**Number**  
493375785

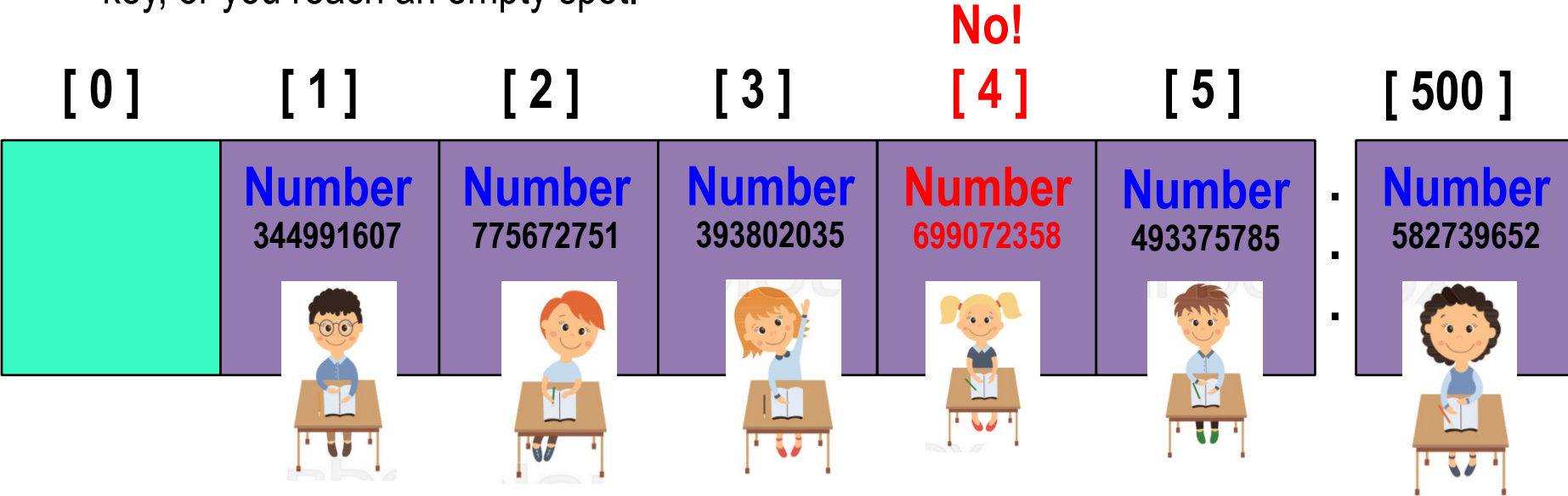


An array of records

# Searching for a Key

- The data (or value) that is attached to a key can be found fairly quickly.
  - $493375785 \bmod 501 = 3$
  - Follow the collision rule (keep moving forward) until you find the key, or you reach an empty spot.

**Number**  
493375785



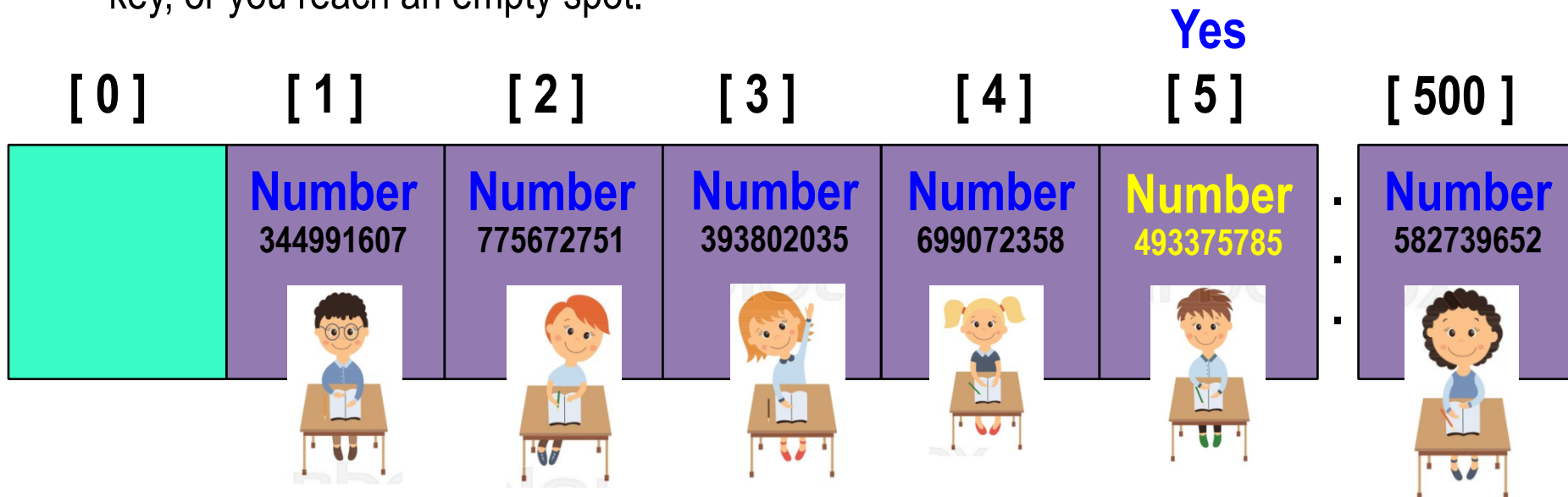
An array of records

# Searching for a Key

- The data (or value) that is attached to a key can be found fairly quickly.

**Number**  
493375785

- $493375785 \bmod 501 = 3$
- Follow the collision rule (keep moving forward) until you find the key, or you reach an empty spot.

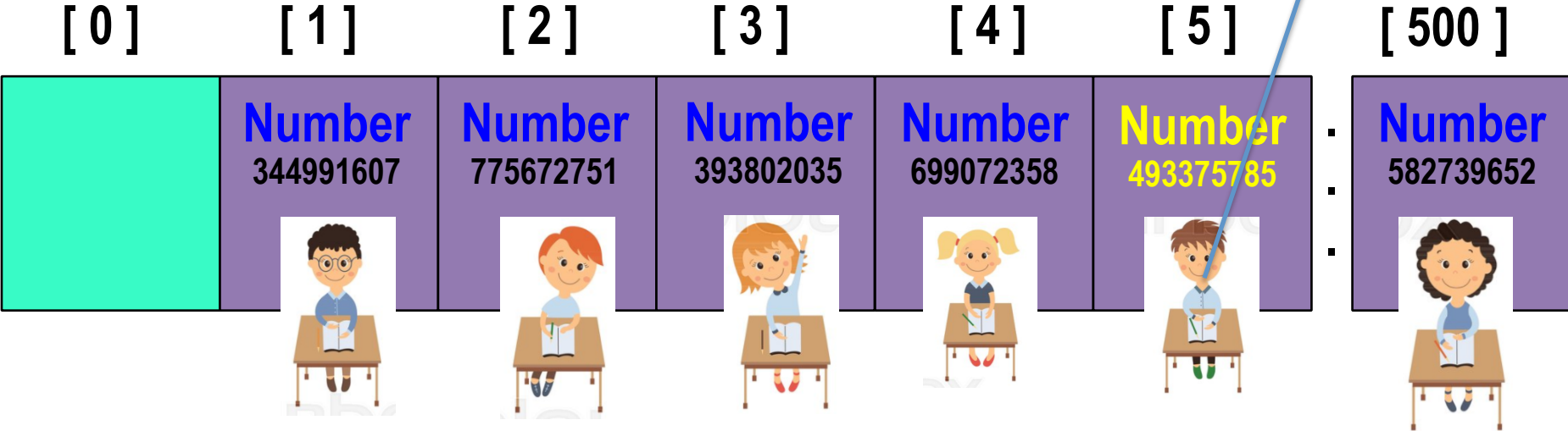


**An array of records**

# Searching for a Key

- The data (or value) that is attached to a key can be found fairly quickly.
  - When the item is found, the information can be copied to the necessary location.

**Number**  
493375785



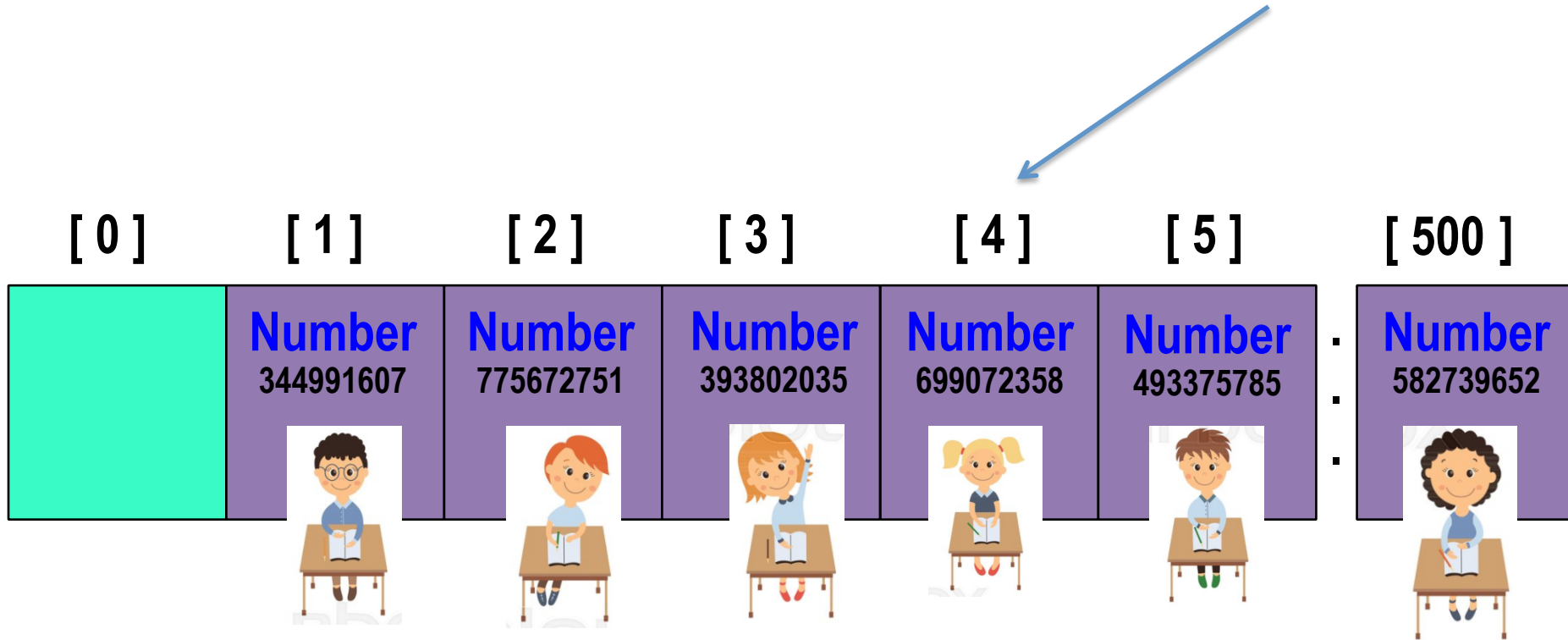
An array of records



# Deleting a Record

- Records may also be deleted from a hash table.

**Delete**  
**699072358**

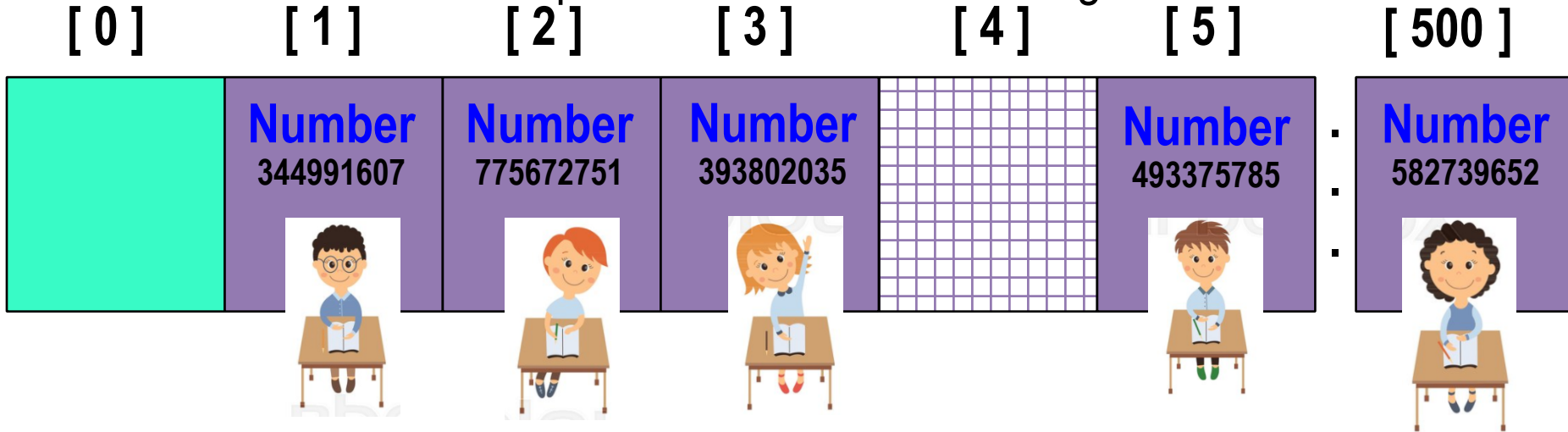


An array of records

# Deleting a Record

- Records may also be deleted from a hash table.
- But the location must not be left as an ordinary "empty spot" since that could interfere with searches.
- The location must be marked in some special way so that a search can tell that the spot used to have something in it.

**Delete**  
**699072358**



**An array of records**

# Map Methods

- Delegate operations to a list-based map at each cell:

**Algorithm** search( $k$ ):

**Output:** The value associated with the key  $k$  in the map, or **null** if there is no entry with key equal to  $k$  in the map

**return**  $A[h(k)].search(k)$  {delegate the search to the list-based map at  $A[h(k)]$ }

**Algorithm** insert( $k, v$ ):

**Output:** If there is an existing entry in our map with key equal to  $k$ , then we return its value (replacing it with  $v$ ); otherwise, we return **null**

$t = A[h(k)].insert(k, v)$  {delegate the put to the list-based map at  $A[h(k)]$ }

**if**  $t = \text{null}$  **then** { $k$  is a new key}

$n = n + 1$

**return**  $t$

**Algorithm** remove( $k$ ):

**Output:** The (removed) value associated with key  $k$  in the map, or **null** if there is no entry with key equal to  $k$  in the map

$t = A[h(k)].remove(k)$  {delegate the remove to the list-based map at  $A[h(k)]$ }

**if**  $t \neq \text{null}$  **then** { $k$  was found}

$n = n - 1$

**return**  $t$

# Interview Question

- Implement Hash Map
  - Hash function just returns the remainder when the key is divided by the hash table size.
  - Hash entry (node) has key and value structure.
  - In addition, the class contains search(key) function to access mapped value by key, insert(key,value) function to put key-value pair in table and remove(key) function to remove hash node by key.
  - For collision resolution, separate chaining strategy could be used.

# Implement Simple Hash Map: testHashMap.cpp

```
1 #include<iostream>
2
3 using namespace std;
4
5 const int TABLE_SIZE = 128;
6
7 // HashEntry Class Declaration
8 class HashEntry
9 {
10     public:
11         int key;
12         int value;
13         HashEntry(int key, int value)
14         {
15             this->key = key;
16             this->value = value;
17         }
18 };
19
20 //HashMap Class Declaration
21 class HashMap
22 {
23     private:
24         HashEntry **table;
25     public:
26         HashMap()
27         {
28             table = new HashEntry * [TABLE_SIZE];
29             for (int i = 0; i< TABLE_SIZE; i++)
30             {
31                 table[i] = NULL;
32             }
33         }
34
35         // Hash Function
36         int HashFunc(int key)
37         {
38             return key % TABLE_SIZE;
39         }
40
```

```
41     void Insert(int key, int value)
42     {
43         int hash = HashFunc(key);
44         while (table[hash] != NULL && table[hash]->key != key)
45         {
46             hash = HashFunc(hash + 1);
47         }
48         if (table[hash] != NULL)
49             delete table[hash];
50         table[hash] = new HashEntry(key, value);
51     }
52
53     // Search Element at a key
54     int Search(int key)
55     {
56         int hash = HashFunc(key);
57         while (table[hash] != NULL && table[hash]->key != key)
58         {
59             hash = HashFunc(hash + 1);
60         }
61         if (table[hash] == NULL)
62             return -1;
63         else
64             return table[hash]->value;
65     }
66
67     // Remove Element at a key
68     void Remove(int key)
69     {
70         int hash = HashFunc(key);
71         while (table[hash] != NULL)
72         {
73             if (table[hash]->key == key)
74                 break;
75             hash = HashFunc(hash + 1);
76         }
77         if (table[hash] == NULL)
78         {
79             cout<<"No Element found at key "<<key<<endl;
80             return;
81         }
82         else
83         {
84             delete table[hash];
85         }
86         cout<<"Element Deleted"<<endl;
87     }
88 }
```

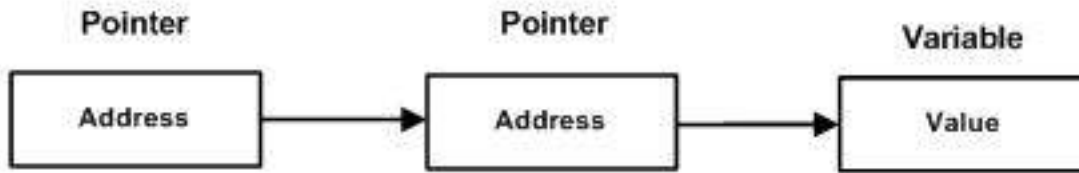
# Implement Simple Hash Map: testHashMap.cpp

```
89     ~HashMap()
90     {
91         for (int i = 0; i < TABLE_SIZE; i++)
92         {
93             if (table[i] != NULL)
94                 delete table[i];
95             delete[] table;
96         }
97     }
98 };
99
100 int main()
101 {
102     HashMap hash;
103     int key, value;
104     int choice;
105     while (1)
106     {
107         cout<<"\n-----"<<endl;
108         cout<<"Operations on Hash Table"<<endl;
109         cout<<"\n-----"<<endl;
110         cout<<"1.Insert element into the table"<<endl;
111         cout<<"2.Search element from the key"<<endl;
112         cout<<"3.Delete element at a key"<<endl;
113         cout<<"4.Exit"<<endl;
114         cout<<"Enter your choice: ";
115         cin>>choice;
116
117         switch(choice)
118         {
119             case 1:
120                 cout<<"Enter element to be inserted: ";
121                 cin>>value;
122                 cout<<"Enter key at which element to be inserted: ";
123                 cin>>key;
124                 hash.Insert(key, value);
125                 break;
126             case 2:
127                 cout<<"Enter key of the element to be searched: ";
128                 cin>>key;
129                 if (hash.Search(key) == -1)
130                 {
131                     cout<<"No element found at key "<<key<<endl;
132                     continue;
133                 }
134             else
135             {
136                 cout<<"Element at key "<<key<<" : ";
137                 cout<<hash.Search(key)<<endl;
138             }
139             break;
140             case 3:
141                 cout<<"Enter key of the element to be deleted: ";
142                 cin>>key;
143                 hash.Remove(key);
144                 break;
145             case 4:
146                 exit(1);
147             default:
148                 cout<<"\nEnter correct option\n";
149         }
150     }
151     return 0;
152 }
```

# Reading C type declarations

- <http://unixwiz.net/techtips/reading-cdecl.html>

# Pointer to the pointer



```
1 #include <iostream>
2
3 using namespace std;
4
5 int main () {
6     int var;
7     int *ptr;
8     int **pptr;
9
10    var = 3000;
11
12    // take the address of var
13    ptr = &var;
14
15    // take the address of ptr using address of operator &
16    pptr = &ptr;
17
18    // take the value using pptr
19    cout << "Value of var :" << var << endl;
20    cout << "Value available at *ptr :" << *ptr << endl;
21    cout << "Value available at **pptr :" << **pptr << endl;
22
23    return 0;
24 }
```



# Why do we use double pointers?



If you want to have a list of characters (a word), you can use `char *word`

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If you want a list of words (a sentence), you can use `char **sentence`



If you want a list of sentences (a monologue), you can use `char ***monologue`



If you want a list of monologues (a biography), you can use `char ****biography`

If you want a list of biographies (a bio-library), you can use `char *****biolibrary`

If you want a list of bio-libraries (a ??lol), you can use `char *****lol`

... ..

*yes, I know these might not be the best data structures*

<https://stackoverflow.com/questions/5580761/why-use-double-pointer-or-why-use-pointers-to-pointers>