

Huffman Codes - Part 2

Note Title

12/1/2009

Announcements

- program due Monday (you are welcome to use Tuesday also)
- Tomorrow - show up!
- Review - Monday in class

Transmitting Information

(See current program!)

A
Send String:
B

From

1000110110101

→ BANANA (For)

Idea

We wish to transmit information using as few bits as possible.

Standard ASCII \rightarrow 8 bits per character

How can we do better?

- Can figure out which characters we actually need.
- More common letters get shorter bitstrings.

First - what do we need?

This sentence contains three a's, three c's, two d's, twenty-six e's, five f's, three g's, eight h's, thirteen i's, two l's, sixteen n's, nine o's, six r's, twenty-seven s's, twenty-two t's, two u's, five v's, eight w's, four x's, five y's, and only one z.

Letters:

A, C, D, E, F, G, H, I, J, K, L, M, N, O, P, R, S, T, U,

(Missing Something... Spaces, Period, comma, apostrophe...)

Frequency Analysis

A	C	D	E	F	G	H	I	L	N	O	R	S	T	U	V	W	X	Y	Z
3	3	2	26	5	3	8	13	2	16	9	6	27	22	2	5	8	4	5	1

Which ones do we want to use few bits for?

OR: which ones can we use many bits for??

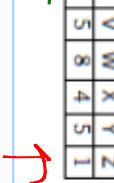
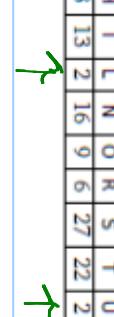
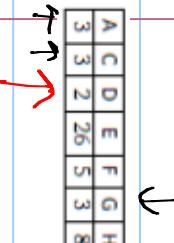
Huffman's algorithm:
Make two least frequent characters

→ merge them into character & recurse

A	C	D	E	F	G	H	I	L	N	O	R	S	T	U	V	W	X	Y	Z
3	3	2	26	5	3	8	13	2	16	9	6	27	22	2	5	8	4	5	1
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take two least frequent



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<tbl_r cells="20" ix="2" maxcspan="

In the end, this:

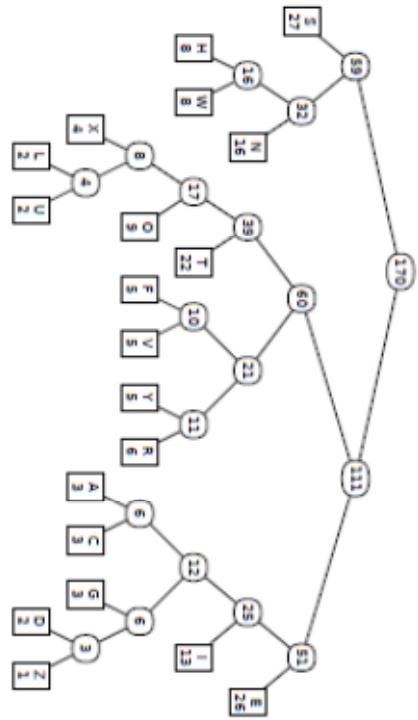
A	C	D	E	F	G	H	I	L	N	O	R	S	T	U	V	W	X	Y	Z
3	3	2	26	5	3	8	13	2	16	9	6	27	22	2	5	8	4	5	1

turns into a decoder tree (like in program)

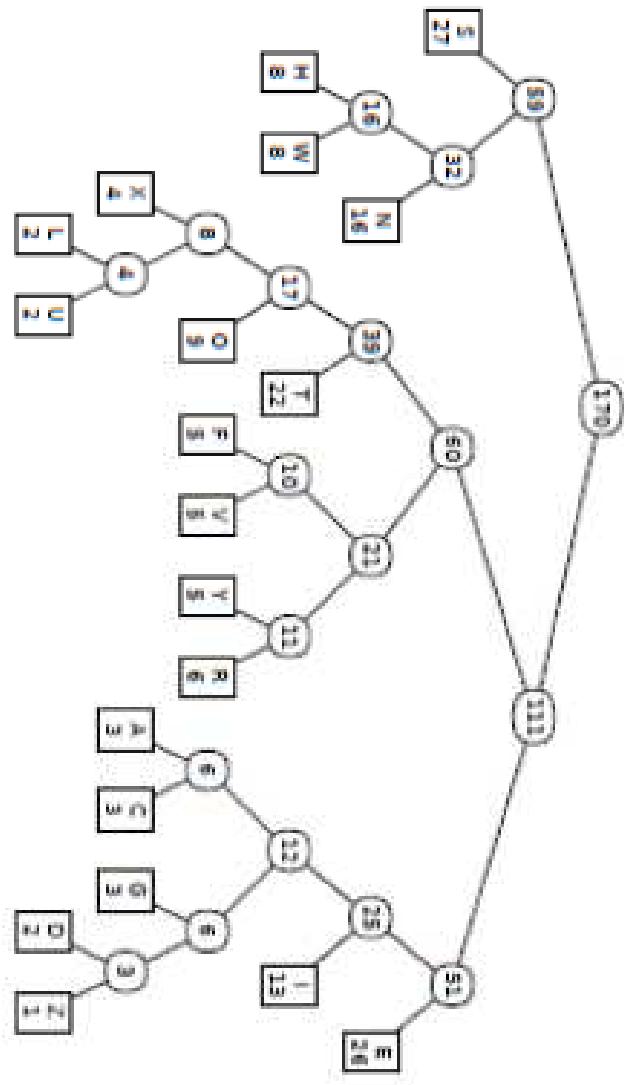
To send an S,
transmit 00,

Original message!

10010100110100001111011100111011100011000101110001000101110011100001101



Exercise: 01001100001010001



Message? HELLO
How many bits? 26 bits

ASCII:
 $8 * 5 = 40$

Code for
SANTA:

00110000
0111001
110000

Why do all this again?

170 letters

This sentence contains three a's, three c's, two d's, twenty-six e's, five f's, three g's, eight h's, thirteen i's, two l's, sixteen n's, nine o's, six r's, twenty-seven s's, twenty-two t's, two u's, five v's, eight w's, four x's, five y's, and only one z.

How does ASCII do?

$$\begin{array}{r} 170 \\ \times 8 \\ \hline 1360 \end{array}$$

Using our tree:

642 bits

(to send tree: 20 char, 8 bits each, 80 bits for tree)